Convex Optimization

Type of Module	Module Code
Advanced Module	АМ-КО

Advanced Module				AM-KO					
Identi Numb	fication er	Workload	Credit Points	Term		Offered Every	Start		Duration
MSc-N	И-КО	270 Hours	9 CP	1. – 3	. Semester	Every two years, WiSe	Winter semester		1 Semester
a) Le		rse Types ecture xercise		Contac	t Time	Private Study 112 h 56 h		Planned Group Size b) 30 Students	
				56 h					
				28 h					
	Exam	Exam preparation				18 h			

2 Module Objectives and Skills to be Acquired

In modern convex optimization, semidefinite optimization occupies a central position. Semidefinite optimization is a generalization of linear optimization, in which linear functions are optimized using positive semidefinite matrices that are subject to linear constraints. A large class of convex optimization problems can be modeled with the help of semidefinite optimization. On the one hand there are solution algorithms for semidefinite Optimizations that are efficient in theory and in practice. On the other hand, semidefinite optimization is a widely used tool of particular elegance.

The aim of the module is to provide an introduction to the theoretical basics, algorithmic techniques and mathematical applications from combinatorics, geometry and algebra. After successful participation, students will be able to

- explain the basic concepts of semidefinite optimization
- give examples from combinatorics, geometry and algebra that can be modeled with the help of semidefinite optimization
- solve semidefinite programs with the help of computer software
- optimization problems to be modeled as semidefinite programs.

Furthermore, the ability to work independently is conveyed with the help of relevant specialist literature. In addition to deepening the lecture material, the exercises also serve to acquire communication and presentation skills.

3 Module Content

- 1. Conical optimization: convex cones, conical programs, duality theory
- 2. Semidefinite optimization: eigenvalue optimization, relaxation of quadratic programs
- 3. The MAXCUT problem: Goemans-Williamson algorithm, Grothendieck inequality
- 4. Packings and colors in graphs: Lovasz theta function, perfect graphs
- 5. Determinant maximization: Loewner-John ellipsoid
- 6. The kiss number problem: The limit of Delsarte, Goethals and Seidel
- 7. Polynomial optimization: sums of squares, sets of positive digits
- 8. Algorithms: interior point method, ellipsoid method

Literature: e.g.

- A. Ben-Tal, A. Nemirovski Lectures on modern convex optimization
- S. Boyd, L. Vandenberghe Convex Optimization
- M. Laurent, F. Vallentin Semidefinite optimization: Theory and applications in combinatorics, geometry, and algebra

Further Literature will be announced in the lecture.

4	Teaching Methods
	Lecture and Exercise
5	Prerequisites (for the Module)
	Formally: None
	Regarding the Contents: Knowledge in the mathematics of Operations Research
6	Type of Examination
	Exam
7	Credits Awarded
	The module is passed and credit points are awarded if the 180-minute final exam is passed or the 30-45-minute oral final exam is passed. The prerequisite for admission to the exam is regular successful completion of the exercises. The respective lecturer announces the exact requirements at the beginning of the event. Registration is required to take the final exam; A resit examination is offered at the beginning of the following semester. Repeated participation in the lecture and the exercises to prepare for a repetition of the final examination is possible. The module is graded.
8	Compatibility with other Curricula
	The module is part of the master courses "Mathematik" and "Wirtschaftsmathematik"
9	Proportion of Final Grade
	9/114
10	Module Coordinator
	Prof. Dr. F. Vallentin